

Menoufiya University  
Faculty of Engineering

Prod. Eng and Mech. Design Dep.

Shebin EL-Kom  
Final First Term Examination  
Academic Year: 2016-2017  
Date: 8-1-2017  
This exam measures ILOS no:(a<sub>1</sub>,a<sub>13</sub>,b<sub>2</sub>,b<sub>6</sub>,b<sub>17</sub>,c<sub>1</sub>,c<sub>3</sub>)

Subject: Vibration of Machines  
Code: PRE 617  
Time Allowed: 3 hours  
Total Marks:100 Marks

Answer all the following Questions:

**Problem (1):**

( 20 Marks )

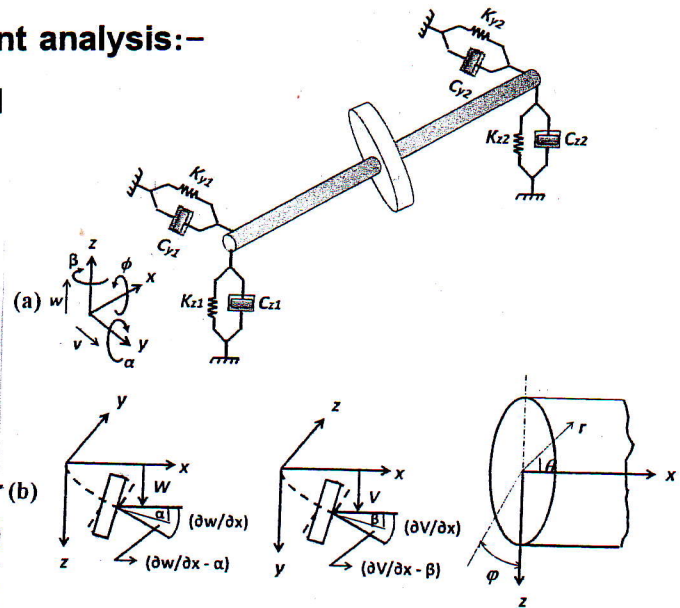
Explain the following parameters and illustrate your answer by Using the experimental and Finite element analysis:-

A-Rotor – bearing system model

- i- Strain energy
- ii- Kinetic energy

B-Quadratic eigenvalue problem

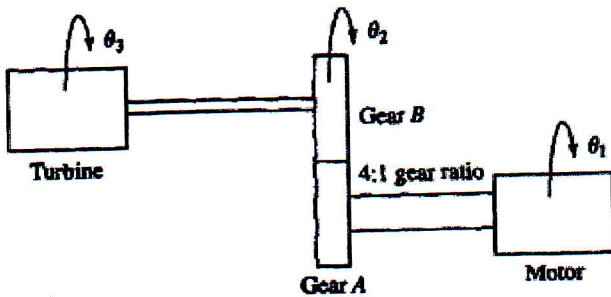
$$-\Omega^2 [M] + i\Omega [C] + [k] X = [0]$$



**Problem (2):**

( 20 Marks )

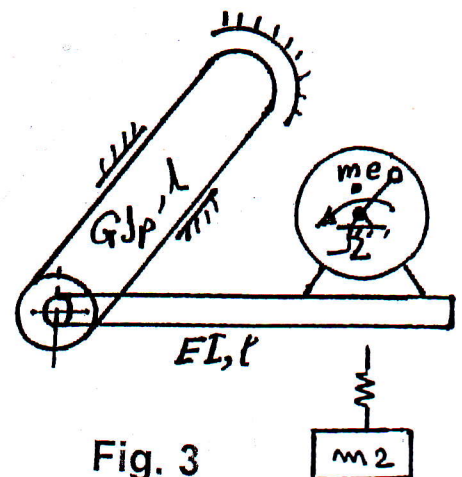
Derive the differential equations governing the torsional oscillations of the turbomotor of Fig. The motor operates at 800 rpm and the turbine shaft turns at 3200 rpm.



Moments of inertia:	Turbine shaft	Motor shaft
Motor 1800 kg · m <sup>2</sup>	G = 80 × 10 <sup>9</sup> N/m <sup>2</sup>	C = 80 × 10 <sup>9</sup> N/m <sup>2</sup>
Turbine 600 kg · m <sup>2</sup>	L = 2.1 m	L = 1.4 m
Gear A 400 kg · m <sup>2</sup>	d = 180 mm	d = 305 mm
Gear B 80 kg · m <sup>2</sup>		

**Problem (3):**

b- A rotor of mass 10 kg and unbalance mo. e = 0.01 kg · m of speed  $\Omega = 5$  sec<sup>-1</sup> is mounted at the end of a set of a two mass-less connected rods of equal length L = 1 m as shown in Fig . If the torsion rigidity of the first rod  $GIp = 1258$  N.m<sup>2</sup> and the flexural rigidity of the second rod  $EI = 1625$  N.m<sup>2</sup> .Design the proper dynamic absorber such that the mass ratio



m2

**Problem 4):**

**(20 Marks)**

Determine the upper and Lower bounds of the fundamental frequency of the system shown in Fig.1 by using:

- (c) Rayleigh,s method
- (d) Dunkarley,s formula
- (e) Bound method

**Problem ( 5 :**

**(15 Marks)**

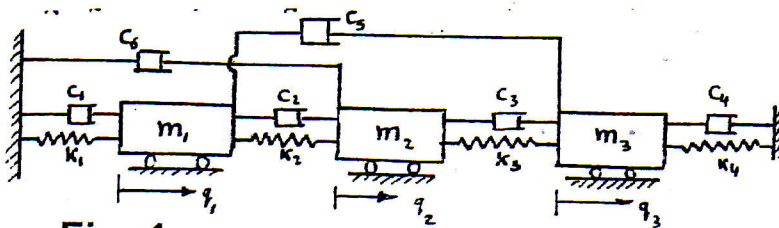
- 1- Express various forms types of Dunkarley,s on the multi-degree system.
  - 2-Estimate the fundamental natural frequency of the beam shown in Fig.2
- All data are given

**Problem ( 6 :**

**(15 Marks)**

Find the eigenvalues and eigenvectors of the matrix using Jacobi method.

$$[D] = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 2 \\ 1 & 2 & 3 \end{bmatrix}$$



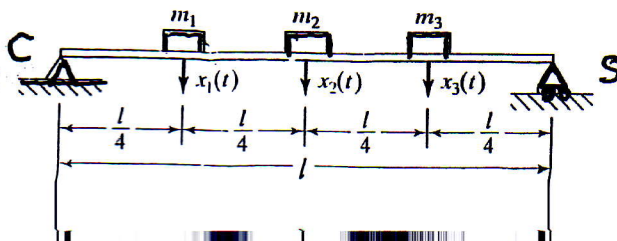
**Fig. 1**

Letting  $m_1 = m_2 = m$  and  $m_3 = 2m$ , we obtain the inertia matrix

$$\tilde{m} = \begin{bmatrix} m_1 & 0 & 0 \\ 0 & m_2 & 0 \\ 0 & 0 & m_3 \end{bmatrix} = m \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 2 \end{bmatrix}.$$

If  $k_1 = k_2 = k_3 = k$  and  $k_4 = 2k$ , the stiffness matrix takes the form,

$$\tilde{k} = \begin{bmatrix} 2k & -k & 0 \\ -k & 2k & -k \\ 0 & -k & 3k \end{bmatrix} = k \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 3 \end{bmatrix}.$$



**Fig. 2**